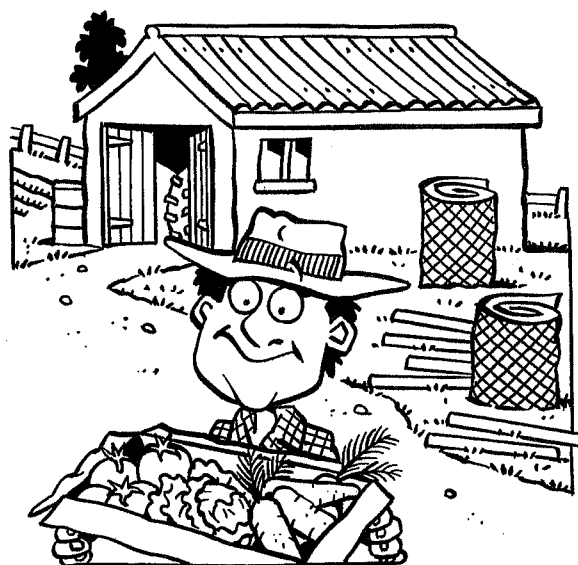


Farmer Sprout's fence

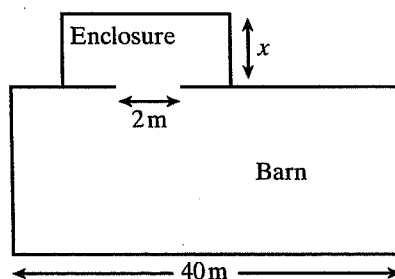
Name:

Due date:/...../.....

Farmer Sprout wishes to create a rectangular enclosure outside his barn, using the barn wall as one side of the enclosure and fencing as the other sides. Entry to the enclosure will be through a door in the barn wall. He wants to use exactly 50 m of fencing.



- 1 The diagram below shows Farmer Sprout's plan for the enclosure.



- What must the total length of the fence be?

- How many sides does the enclosure have?

- Let x represent the width of the enclosure. What is the length of the enclosure if $x = 10$ m?

- Is it possible to have an x value of 13.26 m? Explain. If so, what would be the length of the enclosure for this width?

- Write an expression for the length of the enclosure if the width is x m. Remember to specify the units.


2

[To add borders to a table in Excel select the table cells, right-click, choose Format cells and open the Borders tab.]

Now create a table of possible dimensions for this enclosure in Excel.

- Open a new spreadsheet and set up the table using the headings as shown below. Enter widths of 1.0 m to 26.0 m in column C.

	C	D
3	Possible enclosure dimensions	
4	Width, x (m)	Length (m)
5	1.0	
6	2.0	

- To save time, enter your expression for the length of the enclosure in cell D5. Remember to type 'C5' instead of the x and use '*' for multiply. Use the fill handle  to copy the formula down. (Alternately, you can work out the corresponding lengths and enter them individually.)
- Highlight the values in column C and D, right-click, choose **Format cells** and set the **Category** to **Number** and number of decimal places to '1' on the **Number** tab.
- a If you can, print out your spreadsheet and paste it in the space below.

- b Looking at Farmer Sprout's plan in 1 and the dimensions of the enclosure in your table, would it be practical to build an enclosure with a width less than 5 m? Explain.

- c Is it possible to build an enclosure with a width of 24 m? If so, is it practical?

- d Comment on the lengths you obtained for widths of 25 m and 26 m. What do they mean?


For the remainder of this investigation you will consider enclosures with widths in the range 6.0m to 20.0m.

- Calculate the area of the enclosure for $x = 6.0$ m. Hint: You have the dimensions in your spreadsheet in 2.
- Write an expression for the area of the rectangular enclosure using your answers from 1.
- By substituting $x = 6.0$ m into your expression in 3b, show that the area obtained is the same as in 3a.

- Make a copy of the current sheet by right-clicking the 'Sheet 1' tab at the bottom of the screen. Choose **Move or copy** and check the **Create a copy** box. You should now have two sheets, 'Sheet 1' and 'Sheet 1(2)'. Rename 'Sheet 1(2)' by double-clicking on the tab. Call it 'Area'. Rename 'Sheet 1' as 'Dimensions'.
- Now highlight the rows of your spreadsheet containing widths of 1.0m to 5.0m, right-click and **Delete**. Also delete the rows containing widths of 21.0m to 26.0m. This leaves just dimensions for enclosures with widths of 6.0m to 20.0m.
- Now add an 'Area' heading and column to your table as shown below.

[To write m^2 in Excel, expand the **Font** tab and check the **Superscript** box on the **Format cells** menu, under **Format** tab.]

	C	D	E
3	Possible enclosure dimensions		
4	Width, x (m)	Length (m)	Area, A (m^2)
5	6.0		
6	7.0		

- To save time, enter your expression for the area of the enclosure in cell E5. Remember to type 'C5' instead of the x and use '*' for multiply. Use the fill handle  to copy the formula down. (Alternately, you can work out the corresponding areas and enter them individually.)
 - Format the area values as numbers to 1 decimal place. Paste a copy of your spreadsheet in the space below.
- How does the area change as the value of x increases?

- e Looking at the values in your table, estimate the maximum possible area for the enclosure to the nearest tenth of a square metre.
- f What are the dimensions of the enclosure with the maximum possible area?
- g Make a sketch of the barn and your enclosure in the space below. Mark on the dimensions of the enclosure.

Try
this!

What if Farmer Sprout starts with 30m of fencing instead of 50m? Create a spreadsheet like the one in 3d for widths between 4.0m to 13.0m. Estimate the maximum area that can be enclosed and the dimensions of that enclosure. Paste a copy of your spreadsheet in the space below.

Student comment	Guardian comment/signature	Teacher feedback